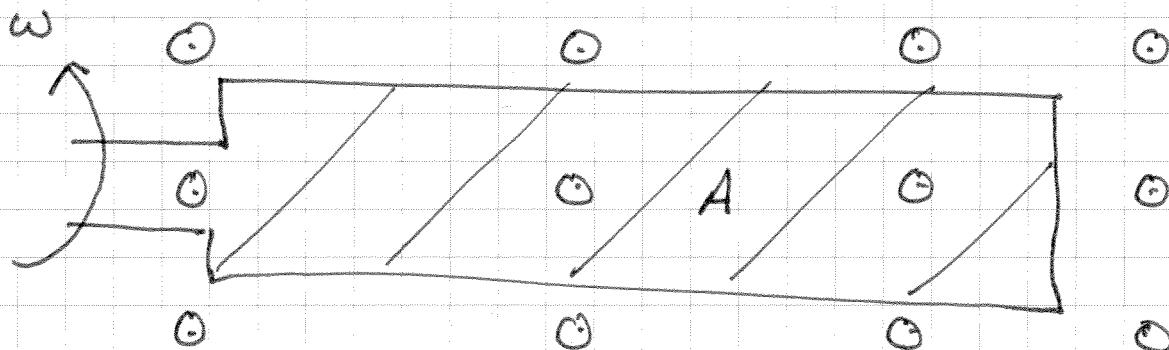


## Electromotive Force III

Generators - Convert mechanical energy into electrical energy.



$$\begin{aligned}\Phi_m &= N \vec{B} \cdot \hat{n} A \\ &= NBA \cos \theta(t)\end{aligned}$$

Period ( $T$ ) - Time for one rotation

Frequency ( $f$ ) - Rotations per second

$$f = \frac{1}{T}$$

$\Rightarrow$  Unit Hertz  $1 \text{ Hz} = 1 \text{ s}^{-1}$

Angular Frequency ( $\omega$ ) -  $\omega = 2\pi f$

If  $\omega$  constant,  $\theta(t) = \theta_0 + \omega t$

$\theta_0$  = Angle between normal and field  
at  $t=0$ .

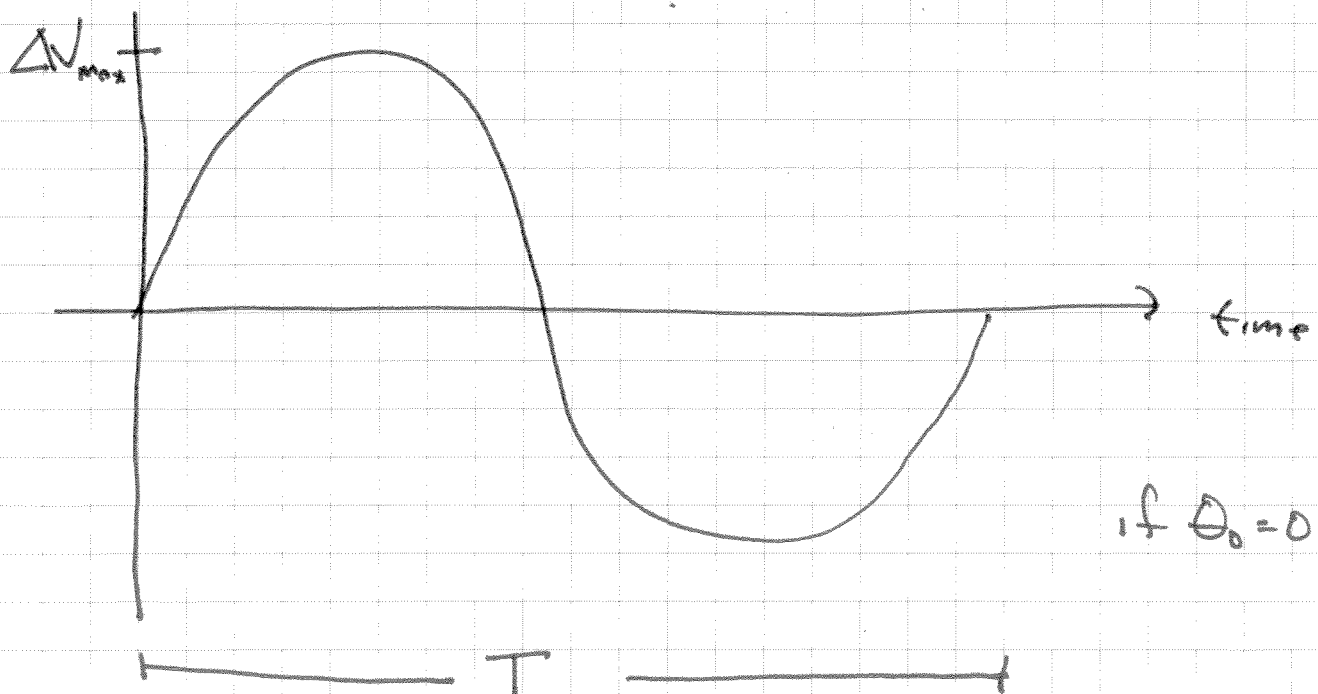
$$\Phi_m = NBA \cos(\theta_0 + \omega t)$$

Flux Rule

$$\text{emf} = - \frac{d\Phi_m}{dt} = NBA\omega \sin(\theta_0 + \omega t)$$

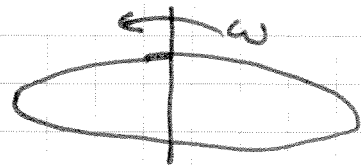
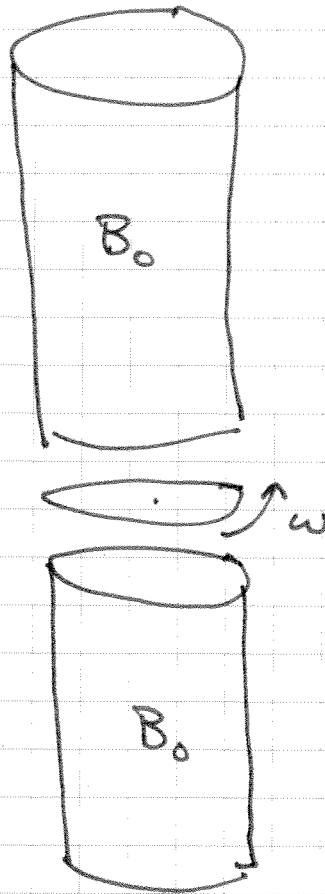
$$= \Delta V_{\text{max}} \sin(\theta_0 + \omega t)$$

$$\Rightarrow \Delta V_{\text{max}} = NBA\omega$$

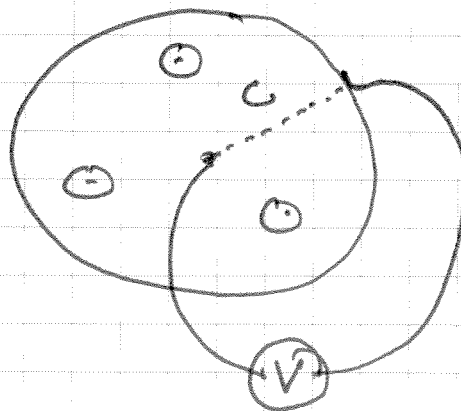


Faraday's Dynamo  
magnetic field.

- Disk spinning in



Top View of Disk



Radius  $R$

## Using Motional Emf along dashed line

$$\text{emf} = \int_C (\vec{v} \times \vec{B}) \cdot d\vec{l} \quad d\vec{l} = ds \hat{s}$$

$$\vec{v} = \omega s \hat{\phi} \quad \vec{B} = B_0 \hat{z}$$

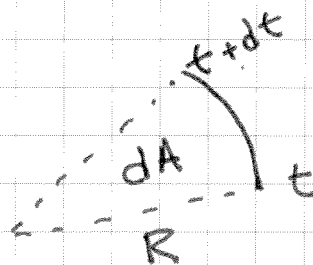
$$\vec{v} \times \vec{B} = \omega s B_0 \hat{\phi} \times \hat{z} = \omega s B_0 \hat{s}$$

$$\text{emf} = \int_C (\vec{v} \times \vec{B}) \cdot d\vec{l} = \omega B_0 \int_0^R s ds$$

$$= \frac{\omega B_0 R^2}{2}$$

## Check with flux rule

In time  $dt$ , the curve  $C$  moving now with the disk describes a wedge



The area of the wedge is

$$dA = \left(\frac{1}{2} R\right)(R d\phi)$$

$$d\Phi_m = B_0 dA = \frac{1}{2} B_0 R^2 d\phi$$

$$|emf| = \left| -\frac{d\Phi_m}{dt} \right| = B_0 \frac{dA}{dt}$$

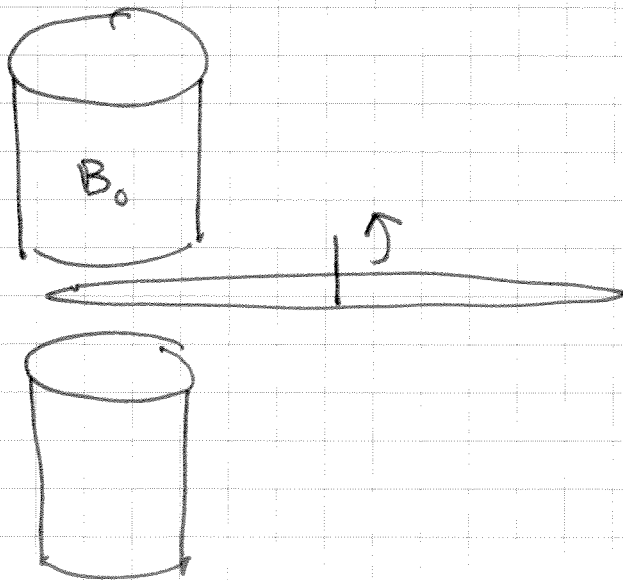
$$= \frac{1}{2} B_0 R^2 \frac{d\phi}{dt} = \frac{1}{2} B_0 R^2 \omega$$

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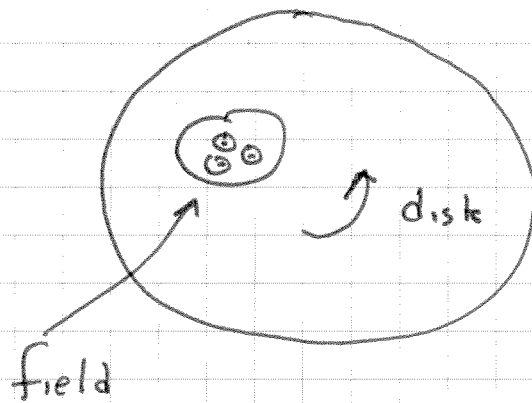
If no load is connected to the dynamo, a region of positive charge will accumulate on the outer edge in a short time producing an electric force that balances the magnetic force. The disk will turn without additional input of energy.

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Now move the disk off center



## Top View



Now the flux through a portion of the conductor is constantly changing; the changing flux induces a current, eddy currents. These currents cause Joule heating. The energy lost to heat slows the disk  $\Rightarrow$  magnetic braking.